

	(D) Neither bounded nor integrable functions on $[a, b]$	
6)	If f is continuous and integrable on $[a, b]$, then there exists a number c between a and b such that.... (A) $\int_a^b f \, dx < (b - c)f(c)$ (B) $\int_a^b f \, dx = (b - c)f(c)$ (C) $\int_a^b f \, dx > (b - c)f(c)$ (D) None of these	(B)
7)	If f is bounded and integrable on $[a, b]$ and k is a number such that $ f(x) \leq k$ for all $x \in [a, b]$, then.... (A) $\left \int_a^b f \, dx \right < k b - a $ (B) $\left \int_a^b f \, dx \right > k b - a $ (C) $\left \int_a^b f \, dx \right \leq k b - a $ (D) None of these	(C)
8)	If P_1 and P_2 are partitions of $[a, b]$ then a partition P is a common refinement of P_1 and P_2 if.... (A) $P \subseteq P_1 \cup P_2$ (B) $P \supseteq P_1 \cup P_2$ (C) $P = P_1 \cup P_2$ (D) None of these	(C)
9)	If p^* is a refinement of a partition P then for a bounded function f ... (A) $L(p^*, f) > L(P, f)$ (B) $L(p^*, f) < L(P, f)$ (C) $L(p^*, f) \geq L(P, f)$ (D) None of these	(C)
10)	If p^* is a refinement of a partition P then for a bounded function f ... (A) $U(p^*, f) \leq U(P, f)$ (B) $U(p^*, f) > U(P, f)$	(A)

	(C) $U(p^*, f) < U(P, f)$ (D) None of these	
11)	The oscillation of a bounded function f in $[a, b]$ is... (A) $\text{Sup } \{ f(\alpha) - f(\beta) : \alpha, \beta \in [a, b]\}$ (B) $\text{Inf } \{ f(\alpha) - f(\beta) : \alpha, \beta \in [a, b]\}$ (C) $\text{Sup } \{ f(x) : x \in [a, b]\}$ (D) $\text{Inf } \{ f(x) : x \in [a, b]\}$	(A)
12)	If P is any partition of $[a, b]$, then for a bounded function f (A) $U(P, f) \geq L(P, f)$ (B) $U(P, f) \leq L(P, f)$ (C) $U(P, f) \neq L(P, f)$ (D) None of these	(A)
13)	If $f(x) = k, \forall x \in [a, b]$ where k is constant then $U(P, f)$ (A) $= k(b - a)$ (B) $> k(b - a)$ (C) $< k(b - a)$ (D) None of these	(A)
14)	If $f(x) = k, \forall x \in [a, b]$ where k is constant then $L(P, f)$ (A) $> k(b - a)$ (B) $= k(b - a)$ (C) $< k(b - a)$ (D) None of these	(B)
15)	If f is bounded and integrable on $[a, b]$, then f is... (A) not integrable on $[a, b]$ (B) integrable on $[a, b]$ (C) constant on $[a, b]$ (D) None of these	(B)

	(C) e -1	(D) 0	
	$\lim_{n \rightarrow \infty} \left(\frac{n^n}{n!} \right)^{\frac{1}{n}} = \dots$		
22)	(A) $\frac{1}{e}$	(B) 0	(D)
	(C) 1	(D) e	
23)	The function $(x) = \frac{1}{2^n} ; \frac{1}{2^{n+1}} < x \leq \frac{1}{2^n} ; (n = 0, 1, 2, \dots)$ and $f(0) = 0$ haspoints of discontinuity.	(A) finite	(C)
	(B) one	(C) infinite	(D) zero
24)	If f and g are integrable on $[a, b]$ and g keeps the same sign over $[a, b]$, then there exists a number μ lying between the bounds of f such that $\int_a^b f(x)dx = \dots$	(A) $> \mu \int_a^b gdx$	(D)
	(B) $< \mu \int_a^b gdx$	(C) $\mu + \int_a^b gdx$	
	(D) $= \mu \int_a^b gdx$		
25)	If $\int_a^b f dx$ and $\int_a^b g dx$ both exists and f is monotone on $[a, b]$, then there exists $\xi \in [a, b]$ such that	(A) $\int_a^b fg dx = f(a) \int_a^\xi g dx + f(b) \int_\xi^b g dx$	(A)
	(B) $\int_a^b fg dx = g(a) \int_a^\xi f dx + f(b) \int_\xi^b g dx$		
	(C) $\int_a^b fg dx = g(a) \int_a^\xi f dx + g(b) \int_\xi^b f dx$		
	(D) $\int_a^b fg dx = f(a) \int_a^b g dx + f(b) \int_a^b g dx$		
26)	If $f(x) = x$ and $g(x) = e^x$ in $[-1, 1]$ then $\int_{-1}^1 f(x)g(x)dx = \dots$	(A) $\frac{e}{2}$	(B)
	(B) $\frac{2}{e}$	(C) $2e$	
	(D) $\frac{4}{e}$		
27)	If $0 < a < b$, then $\left \int_a^b \sin x^2 dx \right $ is ...		(C)

	(A) $\geq \frac{1}{a}$ (C) $\leq \frac{1}{a}$	(B) $\leq \frac{2}{a}$ (D) $\geq \frac{2}{a}$	
28)	For $b \in [0, 1]$, $\int_0^1 \frac{\sin \pi x}{1+x^2} dx = \dots$	(A) $\frac{\pi}{2} \sin \pi b$ (C) $\frac{2}{b^2+1}$	(B) $\frac{2}{\pi} \sin \pi b$ (D) $\frac{\pi}{4} \sin \pi b$
29)	For $\xi \in [a, b]$; $\int_0^1 \frac{\sin \pi x}{1+x^4} dx = \dots$	(A) $\frac{2}{\pi(\xi^2+1)}$ (C) $\frac{4}{\pi(\xi^2+1)}$	(B) $\frac{2}{\pi(\xi^4+1)}$ (D) None of these
30)	If $n > 0$, then $\int_0^{\frac{\pi}{2}} \cos^n x dx = \dots$	(A) proper (C) divergent	(B) improper (D) none of these
31)	For the integral $\int_0^{\frac{\pi}{2}} \frac{1}{\sqrt{\tan x}} dx = \dots$ the points of infinite discontinuity is....	(A) $\frac{\pi}{4}$ (C) Both (A) and (B)	(B) 0 (D) None of these
32)	The integral $\int_0^{\infty} \frac{x^2}{\sqrt{x^5+1}} dx = \dots$	(A) convergent (C) exists	(B) divergent (D) None of these
33)	The integral $\int_0^{\infty} \frac{\sin x}{x^p} dx$ converges absolutely if...	(A) $p < 1$ (C) $p > 1$	(B) $p = 0$ (D) None of these
34)	The integral $\int_a^{\infty} \sin x dx$ is for $X \geq a$.		(A)

	(A) bounded (C) unbounded	(B) not bounded (D) None of these	
35)	The differential equation of the form $(1 - x^2)y'' - 2xy' + n(n + 1)y = 0$; where n a positive integer is called.... (A) Cauchy-Riemann Equation (B) Bernoulli's equation (C) Clairaut's Equation (D) Legendre's equation		(D)
36)	If A and B are arbitrary constants, then the general solution of the equation $(1 - x^2)y'' - 2xy' + n(n + 1)y = 0$ is given by.... (A) $y = AP_n(x) + BQ_n(x)$ (B) $y = A + B$ (C) $y = 0$ (D) $y = 1$		(A)
37)	The expansion of x^3 in terms of Legendre's polynomial is... (A) $2P_3(x) + 3P_1(x)$ (B) $\frac{2}{5}P_3(x) + \frac{3}{5}P_1(x)$ (C) $\frac{2}{5}P_3(x) - \frac{3}{5}P_1(x)$ (D) None of these		(B)
38)	The integral $\int_a^\infty f dx$ converges at ∞ if and only if for every $\varepsilon > 0$ there corresponds a positive number x_0 such that for all $x_1, x_2 \geq x_0$, (A) $\left \int_{x_1}^{x_2} f(x) dx \right < \varepsilon$ (B) $\left \int_a^\infty f(x) dx \right < \varepsilon$ (C) $\left \int_{a+\lambda_1}^{a+\lambda_2} f(x) dx \right < \varepsilon$ (D) None of these		(A)
39)	$P_{2m}(0) = \dots$ (A) 0 (B) 1 (C) $\frac{(-1)^m(2m)!}{2^{2m}(m!)^2}$ (D) $2m$		(C)

	If f is a bounded function on $[a, b]$ then to every $\varepsilon > 0$ there corresponds $\delta > 0$ such that for every partition P of $[a, b]$ with norm $\mu(P) < \delta$	
51)	(A) $U(P, f) < \int_a^b f dx + \varepsilon$ (B) $U(P, f) = \int_a^b f dx + \varepsilon$ (C) $U(P, f) > \int_a^b f dx + \varepsilon$ (D) None of these	(A)
52)	Everyfunction on $[a, b]$ is integrable (A) discontinuous (B) unbounded (C) continuous (D) none of these	(C)
53)	$\lim_{n \rightarrow \infty} \left[\frac{1}{n+1} + \frac{1}{n+2} + \cdots + \frac{1}{n+n} \right] = \dots$ (A) 0 (B) 1 (C) $\log 2$ (D) $\log 2$	(D)