| QN | S.Y.B.SC.(Mathematics) Subject :MTH-302 (A) Algebra Question Bank | Ans |
| :---: | :---: | :---: |
| 1) | Which of the following operations is not binary in $\mathbb{Z}$ ? <br> (A) addition <br> (B) multiplication <br> (C) subtraction <br> (D) division | D |
| 2) | Let $G$ be a non-empty set. A binary operation $*$ on $G$ is said to be ..... if $a *(b * c)=(a * b) * c$ for all $a, b, c \in G$. <br> (A) associative <br> (B) closure <br> (C) commutative <br> (D) abelian | A |
| $3)$ | What is the identity element in the group $(\mathbb{Z},+)$ ? <br> (A) 0 <br> (B) 1 <br> (C) -1 <br> (D) 2 | A |
| 4) | Consider the group $\left(\mathbb{Q}^{+}, *\right)$ where $a * b=\frac{a b}{3}$ for all $a, b \in \mathbb{Q}^{+}$. What is the identity element in $\mathbb{Q}^{+}$? <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) 3 | D |
| 5) | Which of the following is not a group? <br> (A) $(\mathbb{Z},+)$ <br> (B) $(\mathbb{N},+)$ <br> (C) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (D) $G=\mathbb{R}-\{1\}$ under operation $a * b=a+b-a b$ for all $a, b \in G$ | B |
| 6) | Which of the following is incorrect? <br> (A)Identity element in a group is unique. <br> (B) Inverse of every element in a group is unique. <br> (C) Every group is abelian. <br> (D) None of the above. | C |
| 7) | In a group $G=\{1,-1, i,-i\}$ under usual multiplication, $i^{-1}=\ldots \ldots$. <br> (A) 1 <br> (B) -1 <br> (C) $i$ <br> (D) $-i$ | D |


| 8) | In the group $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right), \overline{3}^{-1}=\ldots \ldots$ <br> (A) $\overline{1}$ <br> (B) $\overline{3}$ <br> (C) $\overline{5}$ <br> (D) $\overline{7}$ | B |
| :---: | :---: | :---: |
| 9) | In a group $G$, for $a \in G,\left(a^{-1}\right)^{-1}=\ldots \ldots$ <br> (A) $a$ <br> (B) $a^{-1}$ <br> (C) $e$, identity in $G$ <br> (D) 1 | A |
| 10) | Which of the following is an abelian group? <br> (A) $G=\mathbb{R}-\{1\}$ under operation $a * b=a+b-a b$ for all $a, b \in G$ <br> (B) $G=\{1,-1, i,-i, j,-j, k,-k\}$ the group of quaternions under usual multiplication <br> (C) $G=\{A: A$ is a non-singular matrix of order $n$ over $\mathbb{R}\}$ under usual matrix multiplication <br> (D) $G=\{(a, b): a, b \in \mathbb{R}, a \neq 0\}$ under operation $(a, b) \odot(c, d)=(a c, b c+d)$ for all $(a, b),(c, d) \in G$ | A |
| 11) | Which of the following is a non-abelian group? <br> (A) $(2 \mathbb{Z},+)$ <br> (B) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (C) $G=\mathbb{Q}-\{-1\}$ under operation $a * b=a+b+a b$ for all $a, b \in G$ <br> (D) $G=\{(a, b): a, b \in \mathbb{R}, a \neq 0\}$ under operation $(a, b) \odot(c, d)=(a c, b c+d)$ for $\operatorname{all}(a, b),(c, d) \in G$ | D |
| 12) | Which of the following is a non-abelian group? $(\mathrm{A})(\mathbb{R},+)$ <br> (B) $\left(\mathbb{Z}_{6},+_{6}\right)$ <br> (C) $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right)$ <br> (D) $G=\{A: A$ is a non-singular matrix of order $n$ over $\mathbb{R}\}$ under usual matrix multiplication | D |


| 13) | Which of the following group is finite? <br> (A) $(\mathbb{Z},+)$ <br> (B) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (C) $G=\mathbb{Q}-\{-1\}$ under operation $a * b=a+b+a b$ for all $a, b \in G$ <br> (D) $\left(\mathbb{Q}^{+}, *\right)$ under the operation $a * b=\frac{a b}{2}$ for all $a, b \in \mathbb{Q}^{+}$ | B |
| :---: | :---: | :---: |
| 14) | Which of the following group is infinite? <br> (A) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (B) $\left(\mathbb{Z}_{6},+_{6}\right)$ <br> (C) $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right)$ <br> (D) $\left(\mathbb{Q}^{+}, *\right)$ under the operation $a * b=\frac{a b}{2}$ for all $a, b \in \mathbb{Q}^{+}$ | D |
| 15) | The number of element present in a finite group $G$ is ..... <br> (A) Order of group <br> (B) Order of element <br> (C) Index of group <br> (D) None of the above | A |
| 16) | The order of the group $\left(\mathbb{Z}_{6},+_{6}\right)$ is <br> (A) 2 <br> (B) 3 <br> (C) 5 <br> (D) 6 | D |
| 17) | In the group $(\mathbb{Z},+),(2)^{4}=\ldots$. <br> (A) 0 <br> (B) 2 <br> (C) 8 <br> (D) 16 | C |
| 18) | In the group $\left(\mathbb{Z}_{6},+_{6}\right),(\overline{3})^{-4}=\ldots \ldots$ <br> (A) $\overline{0}$ <br> (B) $\overline{2}$ <br> (C) $\overline{3}$ <br> (D) $\overline{1}$ | A |
| 19) | In the group $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right),(\overline{5})^{4}=\ldots \ldots$ <br> (A) $\overline{1}$ <br> (B) $\overline{3}$ <br> (C) $\overline{5}$ <br> (D) $\overline{7}$ | A |


| 20) | In the group $G=\{1,-1, i,-i\}$ under usual multiplication, order of $i=\ldots \ldots$ <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) 4 | D |
| :---: | :---: | :---: |
| 21) | The number of element in the group $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right)$ of order 4 are <br> (A) 2 <br> (B) 3 <br> (C) 4 <br> (D) 0 | B |
| 22) | Let $G$ be a group and $a, b, c \in G$. Then $(a b c)^{-1}=$ $\qquad$ <br> (A) $a^{-1} b^{-1} c^{-1}$ <br> (B) $c^{-1} a^{-1} b^{-1}$ <br> (C) $c^{-1} b^{-1} a^{-1}$ <br> (D) $a^{-1} c^{-1} b^{1}$ | C |
| 23) | Let $G$ be a group and $a, b \in G$ such that $a b=b a$. Which of the following is incorrect? <br> (A) $a^{k} b=b a^{k}$ for all $k \in \mathbb{N}$ <br> (B) $(a b)^{n}=a^{n} b^{n}$ for all $n \in \mathbb{N}$ <br> (C) $(a b)^{-1}=a^{-1} b^{-1}$ <br> (D) None of the above | D |
| 24) | A group $G$ is called as ...... if the number of element in $G$ is finite? <br> (A) abelian <br> (B) finite <br> (C) infinite <br> (D) non-abelian | B |
| 25) | An Abelian group is also known as ...... group. <br> (A) finite <br> (B) infinite <br> (C) commutative <br> (D) ordered | C |
| 26) | In any group $G, o\left(a^{-1}\right)=$ $\qquad$ <br> (A) $o(a)$ <br> (B) $o(G)$ <br> (C) $\frac{1}{o(a)}$ <br> (D) $\frac{1}{o(G)}$ | A |


| 27) | In the group $(\mathbb{Z},+), o(2)=\ldots \ldots$ <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) infinite | D |
| :---: | :---: | :---: |
| 28) | How many elements in the group $(\mathbb{Z},+)$ has finite order? <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) infinite | A |
| 29) | If $G$ be a group and $a \in G, m, n \in \mathbb{N}$, then $a^{m} a^{n}=$ $\qquad$ <br> (A) $a^{m n}$ <br> (B) $a^{m+n}$ <br> (C) $a^{\frac{m}{n}}$ <br> (D) $a^{(m, n)}$ | B |
| 30) | Order of the identity element in any group is <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) $o(G)$ | B |
| 31) | Let $G$ be a group and $a, b \in G, m \in \mathbb{N}$. Then $\left(b^{-1} a b\right)^{m}=\ldots \ldots$. <br> (A) $b^{-1} a^{m} b$ <br> (B) $b^{-m} a b^{m}$ <br> (C) $b^{-1} a b$ <br> (D) $e$ | A |
| 32) | Which of the following is a improper subgroup of a group $G$ ? $\text { (A) }\{e\}$ <br> (B) $G$ <br> (C) Every subgroup of $G$ <br> (D) None of the above | B |
| 33) | Which of the following is a trivial subgroup of a group $G$ ? $\text { (A) }\{e\}$ <br> (B) $G$ <br> (C) every subgroup of $G$ <br> (D) None of the above | A |


| 34) | A subgroup $H$ of a group $G$ is called $\qquad$ if $H \neq G$. <br> (A) trivial <br> (B) improper <br> (C) proper <br> (D) None of the above | C |
| :---: | :---: | :---: |
| 35) | Which of the following is a subgroup of a group $G=\{1,-1, i,-i\}$ under usual multiplication? <br> (A) $\{1, i\}$ <br> (B) $\{-1,-i\}$ <br> (C) $\{i,-i\}$ <br> (D) $\{1,-1\}$ | D |
| 36) | Which of the following is a not subgroup of the group $(\mathbb{Z},+)$ ? <br> (A) The set of all even integers <br> (B) $n \mathbb{Z}$ for any $n \in \mathbb{N}$ <br> (C) The set of all odd integers <br> (D) $\{0\}$ | C |
| 37) | Consider the statements: <br> I: Union of two subgroup in a group $G$ is a subgroup of $G$. <br> II: Intersection of two subgroup in a group $G$ is a subgroup of $G$ <br> (A) Only statement I is correct <br> (B) Only statement II is correct <br> (C) Both the statements are correct <br> (D) None of the above | B |


| 38) | Let $H, K$ be subgroup of a group $G$. Then $H \cup K$ is a subgroup of $G$ if and only if $(\mathrm{A}) H \subseteq K$ <br> (B) $K \subseteq H$ <br> (C) $H \subseteq K$ or $K \subseteq H$ <br> (D) $H \subseteq K$ and $K \subseteq H$ | C |
| :---: | :---: | :---: |
| 39) | The necessary and sufficient condition for a non-empty subset $H$ of a group $G$ to be a subgroup is that <br> (A) $a, b \in H$ implies $a b^{-1} \in H$ <br> (B) $a, b \in H$ implies $a+b \in H$ <br> (C) $a \in H$ implies $a^{-1} \in H$ <br> (D) $a, b \in H$ implies $a b \in H$ | A |
| 40) | For a dihedral group $D_{6}, o\left(D_{6}\right)=\ldots \ldots$. <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) 6 | D |
| 41) | Consider the following statements: <br> I: Every cyclic group is abelian. <br> II: Every abelian group is cyclic. <br> (A) Only statement I is correct <br> (B) Only statement II is correct <br> (C) Both the statements are correct <br> (D) None of the above | A |
| 42) | The number of generators for the group $G=\{1,-1, i,-i\}$ under usual multiplication are <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) 0 | B |


| 43) | Which of the following group is not cyclic? <br> (A) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (B) $\left(\mathbb{Z}_{6},+_{6}\right)$ <br> (C) $\left(\mathbb{Z}_{8}^{\prime}, \times_{8}\right)$ <br> (D) $(\mathbb{Z},+)$ | C |
| :---: | :---: | :---: |
| 44) | Which of the following group is abelian but not cyclic? <br> (A) $G=\{1,-1, i,-i\}$ under usual multiplication <br> (B) $\left(\mathbb{Z}_{6},+_{6}\right)$ <br> (C) $(\mathbb{Q},+)$ <br> (D) $(\mathbb{Z},+)$ | C |
| 45) | The number of proper subgroup of the group $(\mathbb{Z},+)$ are <br> (A) 1 <br> (B) 2 <br> (C) 5 <br> (D) infinite | D |
| 46) | The number if proper subgroup of the group $\left(\mathbb{Z}_{12},+_{12}\right)$ are <br> (A) 1 <br> (B) 2 <br> (C) 5 <br> (D) 6 | C |
| 47) | A cyclic group of order 10 has ...... number of subgroups. <br> (A) 1 <br> (B) 2 <br> (C) 4 <br> (D) 10 | C |
| 48) | Let $H$ be a subgroup of a group $G$ and $a \in G$. Then the set $\{a h: h \in H\}$ is known as <br> (A) left coset of $H$ by $a$ <br> (B) right coset of $H$ by $a$ <br> (C) coset <br> (D) sub-coset | A |


| 49) | Let $H$ be a subgroup of a group $G$ and $a, b \in G$. Which of the following is incorrect? <br> (A) $a H=H$ if $\in H$. <br> (B) $H a$ and $H b$ are either equal or disjoint. <br> (C) $H a=H b$ implies $a b^{-1} \in H$. <br> (D) None of the above. | D |
| :---: | :---: | :---: |
| 50) | The number of distinct left cosets of a subgroup $H=\{1,-1\}$ in the group $G=\{1,-1, i,-i\}$ under usual multiplication are <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) 4 | B |
| 51) | If $H$ is a subgroup of a finite group $G$, then $o(H) \mid o(G)$. This is the statement of $\qquad$ theorem. <br> (A)Euler's <br> (B) Fermat's <br> (C) Lagrange's <br> (D) Cauchy's | C |
| 52) | If $n \in \mathbb{N}$ and $a \in \mathbb{Z}$ such that $(a, n)=1$, then $a^{\emptyset(n)}=1(\bmod n)$. This is the statement of $\qquad$ theorem. <br> (A) Euler's <br> (B) Fermat's <br> (C) Lagrange's <br> (D) Cauchy's <br> (B) | A |
| 53) | If $p$ is a prime number and $a \in \mathbb{Z}$ such that $p \nmid a$ then $a^{p-1}=1(\bmod p)$. This is the statement of ....... Theorem. <br> (A)Euler's <br> (B) Fermat's <br> (C) Lagrange's <br> (D) Cauchy's | B |
| 54) | Let $G$ be a finite group and $a \in G$. Then $a^{o(G)}=\ldots \ldots$. <br> (A) $e$ <br> (B) $a$ <br> (C) $a^{2}$ <br> (D) $o(G)$ | A |
| 55) | Let $\emptyset(n)$ be an Euler's totient function. Then $\emptyset(10)=$ $\qquad$ <br> (A) 1 <br> (B) 2 <br> (C) 4 <br> (D) 9 | C |
| 56) | Let $\emptyset(n)$ be an Euler's totient function. Then $\emptyset(17)=\ldots \ldots .$. <br> (A) 1 <br> (B) 2 <br> (C) 16 <br> (D) 7 | C |
| 57) | The remainder obtained when $3^{54}$ divided by 11 is $\qquad$ <br> (A) 1 <br> (B) 2 <br> (C) 3 <br> (D) 4 | D |


| 58) | The remainder obtained when $15^{27}$ divided by 8 is $\ldots \ldots$. <br> (A) 1 <br> (B) 2 <br> (C) 6 <br> (D) 7 | D |
| :---: | :---: | :---: |
| 59) | The remainder obtained when $5^{10}-3^{10}$ divided by 11 is $\ldots \ldots$ <br> (A) 0 <br> (B) 1 <br> (C) 3 <br> (D) 5 | A |
| 60) | The number of cyclic subgroups of a group of order $41=\ldots \ldots$ <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) 41 | C |
| 61) | A function $f:(G, *) \rightarrow\left(G_{1}, *^{\prime}\right)$ is called a group homomorphism if $\ldots \ldots$ <br> (A) $f(a * b)=f(a) * f(b)$ for all $a, b \in G$ <br> (B) $f(a * b)=f(a) *^{\prime} f(b)$ for all $a, b \in G$ <br> (C) $f\left(a *^{\prime} b\right)=f(a) *^{\prime} f(b)$ for all $a, b \in G$ <br> (D) $f\left(a *^{\prime} b\right)=f(a)+f(b)$ for all $a, b \in G$ | B |
| 62) | If $f:(G, *) \rightarrow\left(G_{1}, *^{\prime}\right)$ is a group homomorphism and $e, e_{1}$ are identity elements in $G$ and $G_{1}$ respectively, then $f(e)=$ $\qquad$ <br> (A) $e$ <br> (B) $G$ <br> (C) $e_{1}$ <br> (D) 0 | C |
| 63) | If $f:(G, *) \rightarrow\left(G_{1}, *^{\prime}\right)$ is a group homomorphism and $a \in G$, then $f\left(a^{n}\right)=$ $\qquad$ For all $n \in \mathbb{Z}$. <br> (A) $e$ <br> (B) $f(a)^{n}$ <br> (C) $a^{n}$ <br> (D) 0 | B |
| 64) | If $f:(G, *) \rightarrow\left(G_{1}, *^{\prime}\right)$ is a group homomorphism, then the set $\left\{x \in G: f(x)=e_{1}\right.$, identity in $\left.G_{1}\right\}$ is ...... <br> (A) homomorphic image of $G$ <br> (B) kernel of $f$ <br> (C) $f(G)$ <br> (D) $I m f$ | B |
| 65) | Let $G=\{1,-1, i,-i\}$ be the group under usual multiplication. If a function $f:(\mathbb{Z},+) \rightarrow(G, \times)$ defined by $f(n)=i^{n}$ for all $n \in \mathbb{Z}$ is a group homomorphism, then kerf $=$ <br> (A) $\mathbb{Z}$ <br> (B) $\{0\}$ <br> (C) $4 \mathbb{Z}$ <br> (D) $\varnothing$ | C |
| 66) | If a function $f:(\mathbb{R},+) \rightarrow(\mathbb{R},+)$ defined by $f(x)=\frac{x}{2}$ for all $x \in \mathbb{R}$ is a group homomorphism, then $\operatorname{kerf}=$ $\qquad$ <br> (A) $\mathbb{R}$ <br> (B) $\{0\}$ <br> (C) $\mathbb{Z}$ <br> (D) $\varnothing$ | B |
| 67) | A function $g:(\mathbb{R},+) \rightarrow(\mathbb{R},+)$ defined by $g(x)=x+1$ for all $x \in \mathbb{R}$, is $\qquad$ <br> (A) one-one group homomorphism <br> (B) onto group homomorphism <br> (C) not a group homomorphism <br> (D) an isomorphism | C |


| 68) | For $n \in \mathbb{N},(n \mathbb{Z},+) \cong$ $\qquad$ <br> (A) $(\mathbb{R},+)$ <br> (B) $(\mathbb{Q},+)$ <br> (C) $(\mathbb{Z},+)$ <br> (D) $\left(\mathbb{Z}_{n},+_{n}\right)$ | C |
| :---: | :---: | :---: |
| 69) | Every finite cyclic group $G$ of order $n$ is isomorphic to ...... <br> (A) $(\mathbb{R},+)$ <br> (B) $(\mathbb{Q},+)$ <br> (C) $(\mathbb{Z},+)$ <br> (D) $\left(\mathbb{Z}_{n},+_{n}\right)$ | D |
| 70) | Every infinite cyclic group $G$ is isomorphic to ...... <br> (A) $(\mathbb{R},+)$ <br> (B) $(\mathbb{Q},+)$ <br> (C) $(\mathbb{Z},+)$ <br> (D) $\left(\mathbb{Z}_{n},+_{n}\right)$ | C |
| 71) | Consider the following statements: <br> I: Homomorphic image of an abelian group is abelian. <br> II: An isomorphic $f: G \rightarrow G$ is known as automorphism. <br> Which of the following is true? <br> (A) Only statement I is correct <br> (B) Only statement II is correct <br> (C) Both the statements are correct <br> (D) None of the above | C |
| 72) | If $G$ is a cyclic group with generator $a$, then the homomorphic image, $f(G)=\ldots \ldots$. <br> (A) $<a>$ <br> (B) $<f(a)>$ <br> (C) $\{a\}$ <br> (D) $\{e\}$ | B |


| 73) | Which of the following statements is false? <br> $(\mathrm{A})(\mathbb{Z},+) \cong(2 \mathbb{Z},+)$ <br> (B) $G \cong\left(\mathbb{Z}_{4},+_{4}\right)$ where $G=\{1,-1, i,-i\}$ is a group under usual multiplication <br> (C) $(\mathbb{Q},+) \cong(\mathbb{Q}-\{0\}, \times)$ <br> (D) None of the above | C |
| :---: | :---: | :---: |
| 74) | Which of the following statements is false? <br> (A) $(\mathbb{Z},+) \cong(3 \mathbb{Z},+)$ <br> (B) If $G=\{1,-1, i,-i\}$ is a group under usual multiplication, then $G \cong\left(\mathbb{Z}_{4}^{\prime}, \times_{8}\right)$ <br> (C) Any two finite cyclic groups of same order are isomorphic. <br> (C) None of the above | B |
| 75) | If $f: G \rightarrow G_{1}$ is a group isomorphism and $a \in G$, then <br> (A) $o(a)<o(f(a))$ <br> (B) $o(a)>o(f(a))$ <br> (C) $o(a)=o(f(a))$ <br> (D) None of the above | C |
| 76) | Consider $(\mathbb{R},+)$, the group of reals under usual addition and $\left(\mathbb{R}^{+}, \cdot\right)$, the group of positive reals under usual multiplication. Then the $f: \mathbb{R} \rightarrow \mathbb{R}^{+}$defined by $\ldots \ldots$. Is an isomorphism. <br> (A) $f(x)=2^{x}$ for all $x \in \mathbb{R}$ <br> (B) $f(x)=2 x$ for all $x \in \mathbb{R}$ <br> (C) $f(x)=x+2$ for all $x \in \mathbb{R}$ <br> (D) $f(x)=x$ for all $x \in \mathbb{R}$ | A |


| 77) | Let $f: G \rightarrow G^{\prime}$ be a group homomorphism. Consider the following statement: <br> I: $G$ is an abelian group <br> II: $f(G)$ is an abelian group. <br> Which of the following is correct? <br> (A)I implies II only <br> (B) II implies I only <br> (C) I if and only if II <br> (D) Neither I implies II nor II implies I | A |
| :---: | :---: | :---: |
| 78) | Let $f: G \rightarrow G^{\prime}$ be a group homomorphism. Consider the following statement: <br> I: $G$ is a cyclic group <br> II: $f(G)$ is a cyclic group. <br> Which of the following is correct? <br> (A)I implies II only <br> (B) II implies I only <br> (C) I if and only if II <br> (D) Neither I implies II nor II implies I | A |
| 79) | Let $f: G \rightarrow G^{\prime}$ be a group homomorphism. Consider the following statement: <br> I: $G$ is a finite group <br> II: $f(G)$ is a finite group. <br> Which of the following is correct? <br> (A)I implies II only <br> (B) II implies I only <br> (C) I if and only if II <br> (D) Neither I implies II nor II implies I | A |
| 80) | The number of group homomorphisms from the group $(\mathbb{Z},+)$ onto itself $=\ldots .$. <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) infinite | D |


| 81) | A ring $(R,+, \cdot)$ is said to be commutative if ........ <br> (A) $a+b=b+a$ for all $a, b \in R$ <br> (B) $a \cdot b=b \cdot a$ for all $a, b \in R$ <br> (C) $a \cdot b=b \cdot a$ for some $a, b \in R$ <br> (D) $a \cdot b=1$ for all $a, b \in R$ | B |
| :---: | :---: | :---: |
| 82) | Which of the following is not a ring under usual addition and multiplication? <br> (A) $\mathbb{R}$ <br> (B) $\{0\}$ <br> (C) The set of all odd integers <br> (D) $\left\{\frac{p}{q} \in \mathbb{Q}: p, q \in \mathbb{Z}\right.$ and $q$ is odd integer $\}$ | C |
| 83) | Which of the following rings is commutative? <br> (A) $(\mathbb{R},+, \cdot)$ <br> (B) $\left\{\left[\begin{array}{cc}a+i b & c+i d \\ -c+i d & a-i b\end{array}\right]: a, b, c, d \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices <br> (C) The set of $2 \times 2$ matrices over $\mathbb{Z}$ under usual addition and multiplication of matrices <br> (D) None of the above | A |
| 84) | Which of the following rings is without identity? <br> (A) $(2 \mathbb{Z},+, \cdot)$ <br> (B) $\left\{\left[\begin{array}{lll}a & a & a \\ a & a & a \\ a & a & a\end{array}\right]: a \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices <br> (C) $\left\{\frac{p}{q} \in \mathbb{Q}: p, q \in \mathbb{Z}\right.$ and $q$ is odd integer $\}$ under usual addition and multiplication <br> (D) None of the above | A |


| 85) | Which of the following rings is non-commutative? <br> (A) $(2 \mathbb{Z},+, \cdot)$ <br> (B) $\left\{\left[\begin{array}{lll}a & a & a \\ a & a & a \\ a & a & a\end{array}\right]: a \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices <br> (C) The set of $2 \times 2$ matrices over $\mathbb{Z}$ under usual addition and multiplication of matrices <br> (D) None of the above | C |
| :---: | :---: | :---: |
| 86) | Which of the following rings is non-commutative? $(\mathrm{A})(\mathbb{Q},+, \cdot)$ <br> (B) $\left\{\left[\begin{array}{lll}a & a & a \\ a & a & a \\ a & a & a\end{array}\right]: a \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices <br> (C) $\left\{\left[\begin{array}{cc}a+i b & c+i d \\ -c+i d & a-i b\end{array}\right]: a, b, c, d \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices <br> (D) None of the above | C |
| 87) | The identity (unity) element in the ring $\left\{\left[\begin{array}{lll}a & a & a \\ a & a & a \\ a & a & a\end{array}\right]: a \in \mathbb{R}\right\}$ under usual addition and multiplication of matrices is $\qquad$ <br> (A) $\left[\begin{array}{lll}0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0\end{array}\right]$ <br> (B) $\left[\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right]$ <br> (C) $\left[\begin{array}{lll}\frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3}\end{array}\right]$ <br> (D) 1 | C |
| 88) | The identity (unity) element in the ring $(\mathbb{Z}, \oplus, \odot)$ is $\ldots \ldots$, where $a \oplus b=a+b-1$ and $a \odot b=a+b-a b$ for all $a, b \in \mathbb{Z}$. <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) 3 | A |


| 89) | Let $(R,+, \cdot)$ be a ring with identity 1 . Which of the following statement is false? <br> (A) $a \cdot 0=0$ <br> (B) $(-a) b=a(-b)$ <br> (C) $c(a-b)=a c-b c$ <br> (D) $(-1)(-1)=1$ | C |
| :---: | :---: | :---: |
| 90) | The number of units in the ring $\left(\mathbb{Z}_{6},+_{6}, \times_{6}\right)$ are <br> (A) 2 <br> (B) 3 <br> (C) 5 <br> (D) 0 | A |
| 91) | The system $\left(\mathbb{Z}_{6},+_{6}, \times_{6}\right)$ is $\qquad$ <br> (A) not a ring <br> (B) ring but not an integral domain <br> (C) an integral domain but not a field <br> (D) field | B |
| 92) | In the ring $\left(\mathbb{Z}_{7},+_{7}, \times_{7}\right), \overline{3} \times_{7}(-\overline{4})=\ldots \ldots$. <br> (A) $\overline{0}$ <br> (B) $\overline{2}$ <br> (C) $\overline{1}$ <br> (D) $-\overline{2}$ | B |
| 93) | The multiplicative inverse of $1+i$ in the ring $\mathbb{Z}[i]$ is <br> (A) 1 <br> (B) $i$ <br> (C) $1-i$ <br> (D) None of the above | D |
| 94) | The number of zero divisors in the ring $\left(\mathbb{Z}_{6},+_{6}, X_{6}\right)$ are <br> (A) 2 <br> (B) 3 <br> (C) 5 <br> (D) 0 | B |
| 95) | A commutative ring $R$ without zero divisors is called as ....... <br> (A) an integral domain <br> (B) a field <br> (C) a division ring <br> (D) a Boolean ring | A |
| 96) | For $n>1$, a ring $\left(\mathbb{Z}_{n},+_{n}, \times_{n}\right)$ is an integral domain if and only if <br> (A) $n$ is odd <br> (B) $n$ is even <br> (C) $n$ is prime <br> (D) $n$ is composite number | C |


| 97) | Which of the following is not a field? <br> (A) $(\mathbb{C},+, \cdot)$ <br> (B) $(\mathbb{R},+, \cdot)$ <br> (C) $(\mathbb{Q},+, \cdot)$ | (D) $(2 \mathbb{Z},+, \cdot)$ | D |
| :---: | :---: | :---: | :---: |
| 98) | Which of the following is incorrect? <br> (A)Every field is an integral domain. <br> (B) Every integral domain is a field. <br> (C) Every finite integral domain is a field. <br> (D) Every field is a division ring. |  | B |
| 99) | Which of the following rings is a Boolean ring? <br> (A) $(\mathbb{C},+, \cdot)$ <br> (B) $(\mathbb{R},+, \cdot)$ <br> (C) $(\mathbb{Z},+, \cdot)$ | (D) $\left(\mathbb{Z}_{2},+_{2}, x_{2}\right)$ | D |
| 100) | If $R$ is a Boolean ring, then $a^{3}=$ $\qquad$ for all $a \in R$ <br> (A) 0 <br> (B) 1 <br> (C) $a$ <br> (D) $a^{-1}$ |  | C |

