

<p>The Bodwad Sarvajanik Co-Op. Education Society Ltd., Bodwad</p> <p><b>Arts, Commerce and Science College Bodwad</b></p> <p style="text-align: center;"><b><u>Question Bank</u></b></p>		
Class:-SYBSc	Sem:-IV	
Subject: Differential Equations	Paper Name:- MTH 402(A)	
Sr.No.	Questions	Ans
1)	The Wronkian of the function $y_1 = \sin x$ and $y_2 = \sin x - \cos x$ is.... (A) 0                    (B) 1                    (C) $\sin^2 x$ (D) $\cos^2 x$	B
2)	The Wronkian of the function $y_1 = x$ and $y_2 = 2x$ is ..... (A) 0                    (B) 1                    (C) $\sin^2 x$ (D) $\cos^2 x$	A
3)	The Wronskian of the function $y_1 = 3x$ and $y_2 = 2x$ is ..... (A) 0                    (B) 1                    (C) $\sin^2 x$ (D) $\cos^2 x$	A
4)	The Wronkian of the function $y_1 = x^2$ and $y_2 = 2x$ is ..... (A) 0                    (B) 1                    (C) $-3x^2$ (D) $3x$	C
5)	The Wronskian of the function $y_1 = x^2$ and $y_2 = 7x^2$ is ..... (A) 0                    (B) 1                    (C) $-3x^2$ (D) $3x$	A
6)	The Wronskian of the function $y_1 = x^3$ and $y_2 = 2x^3$ is ..... (A) 0                    (B) 1                    (C) $-3x^2$ (D) $3x$	A
7)	The functions $1, x, x^2$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B

8)	The functions $y_1 = x$ and $y_2 = 2x$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
9)	The functions $y_1 = 3x$ and $y_2 = 2x$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
10)	The functions $y_1 = x^2$ and $y_2 = 3x$ , where $x \neq 0$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	A
11)	The functions $y_1 = x^2$ and $y_2 = 7x^2$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
12)	The functions $y_1 = x^3$ and $y_2 = 2x^3$ are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
13)	The Wronskian of $e^{2x} \cos^3 x$ and $e^{2x} \sin^3 x$ is ..... (A) $3e^{4x}$ (B) 0      (C) $3e^{2x}$ (D) $2e^{3x}$	A
14)	Two non-zero functions $f_1(x)$ and $f_2(x)$ of the differential equation are linearly Dependent iff their Wronskian is..... $\forall x \in [a, b]$	A

	(A) zero (c) non vanishing	(B) non-zero (D) none of these	
15)	The Wronskian of functions $e^x$ and $xe^x$ is ..... (A) $e^x$ (B) $e^{2x}$ (C) $xe^x$ (D) $e^{3x}$		<b>B</b>
16)	If S is defined by the rectangle $ x  \leq a,  y  \leq b$ then the functions $f(x,y)=xsiny+ycosx$ satisfy the Lipschitz condition and Lipschitz constant $K= \dots\dots$ (A) a      (B) -1      (C) a+1      (D) b		<b>C</b>
17)	Every continuous function .....satisfy a Lipschitz condition on a rectangle (A) may      (B) must      (C) may not      (D) none of these		<b>C</b>
18)	The wronskian of $y_1(x)$ and $y_2(x)$ is denoted by $W(y_1, y_2)$ and is defined as (A) $W(y_1, y_2) = \begin{vmatrix} y_1 & y_2 \\ y_2 & y_1 \end{vmatrix}$  (B) $W(y_1, y_2) = \begin{vmatrix} y_1 & y_2 \\ x_2 & x_1 \end{vmatrix}$  (C) $W(y_1, y_2) = \begin{vmatrix} x_1 & x_2 \\ y_2 & y_1 \end{vmatrix}$  (D) $W(y_1, y_2) = \begin{vmatrix} y_1 & y_2 \\ y_1 & y_2 \end{vmatrix}$		<b>D</b>
19)	A function $f(x,y)$ is said satisfy Lipschitz's condition in a region D in XY plane if there exists a positive constant K such that $ f(x, y_1) - f(x, y_2)  \leq \dots$ whenever the points $(x, y_1)$ and $(x, y_2)$ both lie in D. (A) $K x_1 - x_2 $ (B) $K y_1 - x_2 $ (C) $K y_2 - y_1 $ (D) $K x_1 - y_2 $		<b>C</b>

20)	<p>Two solutions <math>y_1(x)</math> and <math>y_2(x)</math> of <math>a_0y^{11} + a_1y^1 + a_2y = 0</math>, <math>a_0 \neq 0</math> on <math>(a,b)</math> are Linearly independent if and only if their wronskian is ..... at some point <math>x_0 \in (a, b)</math></p> <p>(A) zero                    (B) not zero                    (C) may or may not zero                    (D) identically zero</p>	B
21)	<p>If <math>W(y_1, y_2) = \begin{vmatrix} 2x^2 &amp; x \\ 4x &amp; 1 \end{vmatrix} = A</math> then value of A is</p> <p>(A) <math>-2x^2</math>                    (B) <math>4x^2</math>                    (C) <math>3x^2</math>                    (D) <math>2x</math></p>	A
22)	<p>If <math>W(y_1, y_2) = \begin{vmatrix} 2x^2 &amp; 3x \\ 4x &amp; 3 \end{vmatrix} = A</math> then value of A is</p> <p>(A) <math>-6x^2</math>                    (B) <math>4x^2</math>                    (C) <math>3x^2</math>                    (D) <math>2x</math></p>	A
23)	<p>If <math>W(y_1, y_2) = \begin{vmatrix} 3x &amp; x \\ 3 &amp; 1 \end{vmatrix} = A</math> then value of A is</p> <p>(A) <math>-2x^2</math>                    (B) <math>4x^2</math>                    (C) <math>3x^2</math>                    (D) <math>0</math></p>	D
24)	<p>If <math>W(y_1, y_2) = \begin{vmatrix} 4x &amp; x \\ 3 &amp; 1 \end{vmatrix} = A</math> then value of A is</p> <p>(A) <math>-6x^2</math>                    (B) <math>4x^2</math>                    (C) <math>3x^2</math>                    (D) <math>0</math></p>	A
25)	<p>If <math>W(y_1, y_2) = \begin{vmatrix} 4x &amp; x \\ 4 &amp; 1 \end{vmatrix} = A</math> then value of A is</p> <p>(A) <math>-2x^2</math>                    (B) <math>4x^2</math>                    (C) <math>3x^2</math>                    (D) <math>0</math></p>	D
26)	<p>If <math>y_1(x)</math> and <math>y_2(x)</math> are any two solutions of <math>a_0(x)y''(x) + a_1(x)y'(x) + a_2(x)y(x) = 0</math>, then the linear combination</p>	C

	<p><math>C_1y_1(x) + C_2y_2(x)</math>, where <math>C_1</math> and <math>C_2</math> are constants, is ..... of the given equation.</p> <p>(A) not solution      (B) may or may not have solution      (C) solution      (D) none of these</p>	
27)	<p>The functions <math>x^2, e^x, e^{-x}</math> are linearly ..... if <math>x = \pm\sqrt{2}</math></p> <p>(A) independent    (B) dependent    (C) congruent      (D) none of these</p>	B
28)	<p>If S is defined by the rectangle <math> x  \leq a,  y  \leq b</math> then the Lipschitz constant for Function <math>f(x,y) = x^2 + y^2</math> is.....</p> <p>(A) b    (B)a    (C) 2b    (D) 2a</p>	C
29)	<p>The Wronskian of <math>\sin x</math> and <math>\cos x</math> is .....</p> <p>(A) 0    (B) 1    (C)-1    (D) 3</p>	C
30)	<p>Taking first and second ratio of simultaneously D.E. <math>\frac{Xdx}{y^2Z} = \frac{dy}{xz} = \frac{dz}{y^2}</math> the Solution of D.E is</p> <p>(A) <math>x^3 + 2y^3 = c_1</math>    (B) <math>x^3 - y^3 = c_1</math>    (C) <math>x^3 + 4y^3 = C_1</math>      D) <math>4x^2 = 5y^2</math></p>	B
31)	<p>One solution of the simultaneous D.E. <math>\frac{dx}{yz} = \frac{dy}{zx} = \frac{dz}{xy}</math> is</p> <p>(A) <math>x^2 = y^2</math>    (B) <math>x^2 - y^2 = c</math>    (C) <math>x^2 - 3y^2 = c</math>    (D)  <math>4x^2 = 5y^2</math></p>	B
32)	<p>Taking first and second fraction of simultaneous D.E</p> <p><math>\frac{dX}{1} = \frac{dy}{2} = \frac{dz}{5z + \tan(y-2x)}</math> is</p> <p>(A) <math>xy = c</math>    (B) <math>x^2 + z^2 = 0</math>    (c) <math>x = 2y + c</math>    (D)  <math>y = 2x + c</math></p>	D
33)	<p>Taking first and third ratio of simultaneously D.E.</p> <p><math>\frac{Xdx}{y^2Z} = \frac{dY}{xz} = \frac{dz}{y^2}</math> the solution of D.E is</p> <p>(A) <math>x^2 + z^2 = c</math>    (B) <math>x^2 - z^2 = c</math>    (C) <math>x^2 + 3y^2 = c</math>      (D) <math>4x^2 + 5y^2 = c</math></p>	B
34)	<p>Solution of simultaneously D.E <math>dx = dy = dz</math> is</p>	C

	(A) $(x - y)(y + z) = c$ (C) $(x - y)(y - z) = c$	(B) $(x + y)(y - z) = c$ (D) $(x + 2y)(y + z) = c$	
35)	Equating the first and second fraction of simultaneous D.E. $dx = dy = dz$ then Solution is (A) $(x - y)(y + z) = c$ (C) $x - y = c$	(B) $y - z = c$ (D) $(x + 2y)(y + z) = c$	C
36)	Equating the second and third fraction of simultaneous D.E $dx = dy = dz$ then solution is (A) $(x - y)(y + z) = c$ (C) $x - y = c$	(B) $y - z = c$ (D) $(x + 2y)(y + z) = c$	B
37)	Equating the first and third fraction of simultaneous D.E. $dx = dy = dz$ then solution is (A) $(x - y)(y + z) = c$ (C) $x - y = c$	(B) $x - z = c$ (D) $(x + 2y)(y + z) = c$	B
38)	Which of the following set of multipliers used to solve simultaneously differential equation $\frac{dX}{Z(X+Y)} = \frac{dY}{Z(X-Y)} = \frac{dZ}{X^2+Y^2}$ (A) $x, y, -z$ and $x, -y, -z$ (C) $y, x, -z$ and $x, -y, -z$	(B) $-x, y, z$ and (D) $y, x, z$ and $x, y, -z$	C
39)	Equating first and second ratio of simultaneous differential equation $\frac{dX}{x} = \frac{dy}{y} = \frac{dz}{z}$ , then $\log x =$ (A) $\log y + c$ (B) $\log cy + c$ (C) $\log(x + y) + c$ (D) $\log\left(\frac{x}{y}\right) + c$		A
40)	Equating first and second ratio of simultaneous differential equation		B

	$\frac{dx}{x} = \frac{dy}{y} = \frac{dz}{z}$ , then $\log x =$ (A) $\log y$ (B) $\log cy$ (C) $\log(x + y)$ (D) $\log\left(\frac{x}{y}\right)$	
41)	<p>Choosing multipliers a,b,1 for simultaneous differential equation</p> $\frac{dX}{y} = \frac{dy}{-x} = \frac{dz}{bX - ay}$ , then we get (A) $aX + by = C_1$ (B) $X + Y + Z = C_1$ (C) $aX - y + Z = C_1$ (D) $aX + by + Z = C_1$	<b>D</b>
42)	<p>Which of the following set of multipliers for simultaneous differential equation <math>\frac{dx}{mz - ny} = \frac{dy}{nx - lz} = \frac{dz}{ly - mx}</math></p> <p>(A) <math>x, y - z</math> and <math>1, 0, 0</math>          (B) <math>-x, y, z</math> and <math>l, -m, -n</math>          (C) <math>y, x, -z</math> and <math>1, 1, 1</math>          (D) <math>x, y, z</math> and <math>l, m, n</math></p>	<b>D</b>
43)	<p>If <math>\frac{dx}{P} + \frac{dy}{Q} + \frac{dz}{R} = \frac{A}{lP + mQ + nR}</math>, then <math>A =</math></p> <p>(A) <math>ldx + mdy + ndz</math>          (B) <math>mdx + ldy + ndz</math>          (C) <math>ldx - mdy + ndz</math>          (D) <math>ldx + mdy - ndz</math></p>	<b>A</b>
44)	<p>If <math>\frac{dx}{P} + \frac{dy}{Q} + \frac{dz}{R} = \frac{xdx + ydy + zdz}{A}</math>, then <math>A =</math></p> <p>(A) <math>xP + yQ + zR</math>          (B) <math>xP - yQ + zR</math>          (C) <math>xP + yQ - zR</math>          (D) <math>yP - xQ + zR</math></p>	<b>A</b>

	The solution of simultaneous differential equation $\frac{dX}{a} = \frac{dy}{a} = dZ$ is (A) $(x - ay)(y + z) = c$ (B) $(x + ay)(y - z) = c$ (C) $(x - y)(y - az) = c$ (D) $(x + ay)(y + az) = c$	C
46)	Taking first and second ratio of simultaneous D.E. $\frac{dX}{xy} = \frac{dy}{y^2} = \frac{dz}{zxy - 2x^2}$ is (A) $xy = c$ (B) $x^2 + z^2 = 0$ (C) $x - y = c$ (D) $\frac{dX+dy}{2+x+y}$	D
47)	Using multipliers 1,1,0 to $\frac{dX}{1+y} = \frac{dy}{1+x} = \frac{dz}{z}$ then each fraction is equal to (A) $\frac{dX+dZ}{2+x+z}$ (B) $\frac{dX+dy}{1+x+y}$ (C) $\frac{dx+dy}{2+y}$ (D) $\frac{dX+dy}{2+x+y}$	D
48)	One solution of the simultaneous D.E $\frac{dX}{yz} = \frac{dy}{zx} = \frac{dz}{xy}$ is (A) $x^2 - z^2 = c$ (B) $x^2 + z^2 = 0$ (C) $x^2 - 3y^2 = 0$ (D) $x^2 = 5y^2 + 2$	A
49)	Which of the following is true in the Pfaffian different equation $xdx + ydy + zdz = 0$ (A) $\frac{\partial P}{\partial y} = \frac{\partial Q}{\partial x}$ (B) $\frac{\partial P}{\partial z} = \frac{\partial R}{\partial x}$ (C) $\frac{\partial R}{\partial y} = \frac{\partial Q}{\partial z}$ (D) All above	D
50)	If P,Q,R are homogeneous function of x,y,z of same degree n in Pfaffian	B





	(A) $2x^2$ (C) z	(B) $3y^2$ (D) $x^3$	
63)	The differential equation $2x^2ydx + 3xy^2dy + zdz = 0$ , i.e. $Pdx + Qdy + Rdz = 0$ then value of $\frac{\partial Q}{\partial x}$ is ..... (A) $2x^2$ (C) z	(B) $3y^2$ (D) $x^3$	<b>B</b>
64)	The differential equation $2x^2ydx + 3xy^2dy + zdz = 0$ , i.e. $Pdx + Qdy + Rdz = 0$ then value of $\frac{\partial R}{\partial x}$ is ..... (A) $2x^2$ (C) z	(B) $3y^2$ (D) 0	<b>D</b>
65)	The differential equation $2x^2ydx + 3xy^2dy + zdz = 0$ , i.e $Pdx + Qdy + Rdz = 0$ then of $\frac{\partial P}{\partial z}$ is ..... (A) $2x^2$ (C) $3xy^2$	(B) $x^2z - y^3$ (D) $x^3$	<b>D</b>
66)	The differential equation $(x^2z - y^3)dx + 3xy^2dy + x^3dz = 0$ , i.e $Pdx + Qdy + Rdz = 0$ then value of R is ..... (A) $y^3$ (C) $3xy^2$	(B) $x^2z - y^3$ (D) $x^3$	<b>D</b>
67)	The value of $\frac{\partial P}{\partial y}$ in the differential equation $(y - Z)(Y + Z - 2x)dx + (z + x - 2y)dy + (x - y)(x + y - 2z)dz = 0$ is ..... (A) $2y - 2x$ (C) $x - z$	(B) $2x - 3y$ (D) $2z + 3y$	<b>A</b>

68)	The differential equation $Pdx + Qdy + Rdz = 0$ is ..... If it satisfies the conditions $\frac{\partial P}{\partial y} = \frac{\partial Q}{\partial x}$ , $\frac{\partial Q}{\partial z} = \frac{\partial R}{\partial y}$ and $\frac{\partial R}{\partial x} = \frac{\partial P}{\partial z}$ (A) exact (B) not exact (C) may or may not be exact (D) none of these	A
69)	An equation of the form $Pdx + Qdy + Rdz = 0$ , where P,Q, R are function of x, y (A) simultaneous differential equation (B) Pfaffian differential equation (C) linear equation (D) non-linear equation	B
70)	Which of the following is true in the Pfaffian differential Equation $(y + z)dx + dy + dz = 0$ (A) $\frac{\partial P}{\partial y} = \frac{\partial Q}{\partial x}$ (B) $\frac{\partial P}{\partial z} = \frac{\partial R}{\partial x}$ (C) $\frac{\partial R}{\partial y} = \frac{\partial Q}{\partial z}$ (D) All above	C
71	Which of the following set of multipliers for simultaneous differential equation $\frac{dx}{x(y-z)} = \frac{dy}{y(z-x)} = \frac{dz}{z(x-y)}$ (A) $x, y - z$ and $1, 0, 0$ (B) $1/x, 1/y, 1/z$ and $1, 1, 1$ (C) $y, x, -z$ and $1, 1, 1$ (D) $x, y, z$ and $l, m, n$	B
72	$xdy + ydx = d(xy)$ A) True B) False	A
73	$[xdy - ydx]/(x^2) = d(x/y)$ A) True B) False	A
74	$[xdy - ydx]/(xy) = d(\log(x/y))$	A

	A)True B)False	
75	$Xdy - ydx = d(xy)$ A)True B)False	B
76	$[xdy - ydx]/(x^2) = d(y/x)$ A)True B)False	B
77	$[xdy - ydx]/(xy) = d((x/y))$ A)True B)False	B
78	$[xdy - ydx]/(xy) = d(\log(y/x))$ A)True B)False	B
79	$[xdy - ydx]/(x^2 + y^2) = d(\tan^{(-1)}(y/x))$ A)True B)False	A
80	$[xdy - ydx]/(x^2 + y^2) = d(\tan^{(-1)}(x/y))$ A)True B)False	B
81	The differential equation $Pdx + Qdy + Rdz = 0$ is exact then it is integrable. A)True B)False	A
82	The differential equation $Pdx + Qdy + Rdz = 0$ is exact then it is not integrable. A)True B)False	B
83	The functions 1, x, 2x are ..... (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
84	Which of the following set of multipliers for simultaneous differential equation $\frac{yzdx}{(y-z)} = \frac{zx dy}{(z-x)} = \frac{xy dz}{(x-y)}$ (A) x, y - z and 1,0,0 (B) 1/x, 1/y, 1/z and 1,1,1 (C) 1/yz, 1/zx, 1/xy and 1,1,1	C

	(D) $x, y, z$ and $l, m, n$	
85	<p>Which of the following set of multipliers for simultaneous differential equation <math>\frac{adx}{bc(y-z)} = \frac{bdy}{ca(z-x)} = \frac{cdz}{ab(x-y)}</math></p> <p>(A) <math>ax, by, cz</math> and <math>a,b,c</math></p> <p>(B) <math>1/x, 1/y, 1/z</math> and <math>1,1,1</math></p> <p>(C) <math>1/yz, 1/zx, 1/xy</math> and <math>1,1,1</math></p> <p>(D) <math>x, y, z</math> and <math>l, m, n</math></p>	A
86	<p>Which of the following set of multipliers for simultaneous differential equation</p> $\frac{dx}{x(2y^4 - z^4)} = \frac{dy}{y(z^4 - zx^4)} = \frac{dz}{z(x^4 - y^4)}$ <p>(A) <math>1/x, 1/y, 2/z</math> and <math>x^3, y^3, z^3</math></p> <p>(B) <math>1/x, 1/y, 1/z</math> and <math>1,1,1</math></p> <p>(C) <math>1/yz, 1/zx, 1/xy</math> and <math>1,1,1</math></p> <p>(D) <math>x, y, z</math> and <math>l, m, n</math></p>	A
87	<p>Which of the following set of multipliers for simultaneous differential equation</p> $\frac{dx}{x(y^2 - z^2)} = \frac{dy}{-y(z^2 + x^2)} = \frac{dz}{z(x^2 + y^2)}$ <p>(A) <math>-1/x, 1/y, 1/z</math> and <math>x, y, z</math></p> <p>(B) <math>1/x, 1/y, 1/z</math> and <math>1,1,1</math></p>	A

	(C) $1/yz, 1/zx, 1/xy$ and $1,1,1$  (D) $x, y, z$ and $l, m, n$	
88	The functions $\cos 2x, \sin 2x$ are .....  (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	A
89	The functions $\cos 2x, 4\cos 2x$ are .....  (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
90	The functions $x^2, e^x, e^{4x}$ are .....  (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	A
91	The functions $\sin 2x, 4\sin 2x$ are .....  (A) Linearly Independent (B) Linearly Dependent (C) Linearly Independent and Linearly Dependent (D) None of these	B
92	In variation parameter method for second order DEq we have to assume that $y = Au + BV$ A) True B) False	A
93	In variation parameter method for second order DEq is useful for finding Particular Integral A) True B) False	A
94	Forward differential operator $\Delta$ is defined as $\Delta f(x) = f(x + h) - f(x)$	A

	A)True B)False	
95	Forward differential operator $\Delta$ is defined as $\Delta = E - 1$ . A)True B)False	<b>A</b>
96	Operator $Ef(x) = f(x+h)$ A)True B)False	<b>A</b>
97	Operator $E^2 f(x) = f(x+2h)$ A)True B)False	<b>A</b>
98	Forward differential operator $\Delta$ is defined as $\Delta = E + 1$ . A)True B)False	<b>B</b>
99	$E^3 f(x) = f(x+3h)$ A)True B)False	<b>A</b>
100	$E^3 f(x) = f(x-3h)$ A)True B)False	<b>B</b>
101	$\Delta^2 = E^2 - 2E + 1$ . A)True B)False	<b>A</b>