| Q.N. | TYBSc(Mathematics) Subject : MTH 503: Algebra Question Bank | Ans |
| :---: | :---: | :---: |
| 1) | A subgroup $H$ of a group $G$ is called a normal subgroup of $G$ if... <br> a) $H a=H a^{-1}, \forall a \in G$ <br> b) $H a=a H, \forall a \in G \quad$ c) $H a=$ <br> $a^{-1} H$, for some $a \in G$ <br> d) $H a=a H^{-1}, \forall a \in G$ | (B) |
| 2) | Read the following statement and choose the correct option. Statement: The kernel of a group homomorphism is always a normal subgroup. This statement is <br> (A) True (B) False <br> (C) Not relevant (D) None of these | (A) |
| 3) | A normal subgroup is also called ... <br> (A) invariant subgroup (B) self-conjugate subgroup <br> $(C)$ both $(A)$ and $(B)(D)$ none of these | (C) |
| (4) | A group $G \neq\{e\}$ is called a $\qquad$ if the only normal subgroups of $G$ are $\{e\}$ and G. <br> (A) simple group (B) finite group <br> (C) infinite group (D) quotient group | (A) |
| (5) | Let $G$ be a group. The subgroup of $G$ whose members are finite products of elements of the form $a b a^{-1} b^{-1}, a \in G$ and $b \in G$ is called the .... <br> (A) Commutative subgroup (B) Commutator subgroup <br> (C) Non Commutator Subgroup (D) None of these | (B) |
| (6) | A group $G$ is an abelian group if and only if the commutator subgroup of $G$ is the ... <br> (A) Trivial group (B) Non-trivial group <br> (C) Both (A) and (B) (D) None of these | (A) |
| (7) | Read the following statement and choose the correct option. <br> Statement: The commutator subgroup of a group is a normal subgroup. <br> This statement is <br> (A) True (B) False <br> (C) Irrelevant (D) None of these | (A) |
| (8) | Read the following statement and choose the correct option. <br> Statement: The commutator subgroup of a group is not a normal subgroup. <br> This statement is <br> (A) True (B) False <br> (C) Irrelevant (D) None of these | (B) |
| (9) | Let $G$ be a group and $G^{\prime}$ the commutator subgroup of $G$. Then $G / G^{\prime}$ is... <br> (A) Abelian group (B) Non abelian group | (A) |


|  | (C) Not a quotient group (D) None of these |  |
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| (10) | Let $H$ be a subgroup of a group $G$ and $a \in G$. Then, the right coset of $H$ in a group $G$ is given by <br> (A) $a H=\{h a / h \in H\} \quad$ (B) $H a=a h / h \in H$ <br> (C) $H a=\{h e / h \in H, e \in G\}$ <br> (D) $H a=\{h a / h \in H\}$ | (D) |
| (11) | Let $G=\mathbb{Z}$ (group) and its subgroup $H=3$. Then the quotient group $\mathrm{G} / \mathrm{H}$ is... <br> (A) $\mathbb{Z}_{3}(B) \mathbb{Z}$ <br> (C) $3 \mathbb{Z}$ (D) Not exist | (A) |
| (12) | Consider the group $\mathrm{Z}_{12}$ with addition modulo $\bigoplus_{12}$ and let $H$ $=\{0,3,6,9\}$. Then $H$ is a subgroup of $G$ and the elements of left coset $8+H$ are... <br> (A) $\{0,3,6,9\}$ (B) $\{0,1,2,3,4,5,6,7,8,9,10,11\}$ <br> (C) $\{2,5,8,11\}$ <br> (D) $\{8,11,14,17,0\}$ | (C) |
| (13) | $a * H=H * a$ relation holds if $H$ is <br> (A) a semigroup of an abelian group (B) a cyclic group <br> (C) a monoid of a group (D) a subgroup of an abelian group | (D) |
| (14) | If G is a finite group and $N$ is a normal subgroup of $G$ then $0(G / N)=\ldots$. <br> (A) $\frac{o(G)}{o(N)}$ <br> (B) $\frac{o(N)}{o(G)}$ <br> (C) $) \frac{o(G)}{o(H)}$ <br> (D)does not exist | (A) |
| (15) | Read the following statements and choose the correct option. Statement I: If $G$ is an abelian group then so would be any of its quotient group is an abelian group. <br> Statement II: We can have an abelian quotient group, without the 'parent' group being an abelian. <br> (A) Only statement I is true (B) Only statement II is true <br> (C) Both (A) and (B) are true (D) None of these | (C) |
| (16) | Let $G$ and $G^{\prime}$ be isomorphic. If $G$ is an abelian group, so $G^{\prime}$ is... <br> (A) non-abelian group (B) an abelian group <br> (C) finite group (D) none of these | (B) |
| (17) | Let $\theta: G \rightarrow G^{\prime}$ be an isomorphism of $G$ onto $G^{\prime}$. Let $e$ and $e$ ' be the unit elements of $G$ and $G^{\prime}$ respectively. Then <br> (A) $\theta(e)=e^{\prime}$ (B) $\theta(e)=e$ <br> (C) $\theta(e)=0$ (D) $\theta(0)=e^{\prime}$ | (A) |
| (18) | Let $\theta: G \rightarrow G^{\prime}$ be an isomorphism of $G$ onto $G^{\prime}$. Let $e$ and $e$ ' be the unit elements of $G$ and $G^{\prime}$ respectively. Then for any $a \in$ $G$, <br> (A) $\theta\left(a^{-1}\right)=e$ (B) $\theta\left(a^{-1}\right)=e^{\prime}$ <br> (C) $\theta\left(a^{-1}\right)=a$ (D) $\theta\left(a^{-1}\right)=[\theta(a)]^{-1}$ | (D) |
| (19) | Let $\theta: G \rightarrow G^{\prime}$ be a homomorphism of $G$ onto $G^{\prime}$ and let $K$ $=\operatorname{ker} \theta$. Then $K$ is a normal subgroup of $G$ and $G / K=$ $\qquad$ <br> (A) $G^{\prime}$ (B) $G$ <br> (C) $K(\mathrm{D})$ None of these | (A) |


| (20) | Any infinite cyclic group is isomorphic to <br> (A) $Z$ <br> (B) $Z_{n}$ <br> (C) $Z / n$ <br> (D) $Z / n Z$ | (A) |
| :---: | :---: | :---: |
| (21) | If $f: G \rightarrow G^{\prime}$ be an onto homomorphism with $K=\operatorname{Ker} f$, then $\ldots$. <br> (A) $\frac{G}{K} \cong G(\mathrm{~B}) \frac{G}{K} \cong G^{\prime}$ <br> (C) $\frac{G}{K} \neq G^{\prime}$ (D) none of these | (B) |
| (22) | Let $S$ be a non-empty set. Any. mapping $f: S \rightarrow S$ is called a permutation. <br> (A) one-one, onto (B) many-one, onto <br> (C) one-one, into (D) many-one, into | (A) |
| (23) | An $\qquad$ of $G$ onto itself is called an $\ldots \ldots$ of $G$, where $G$ is a group. <br> (A) automorphism, isomorphism (B) homomorphism, automorphism <br> (C) isomorphism, automorphism (D) none of thes | (C) |
| (24) | Any finite cyclic group of order $n$ is isomorphic to <br> (A) $Z$ (B) $Z_{n}$ <br> (C) $Z / n$ (D) none of these | (B) |
| (25) | Permutation is a $\qquad$ mapping. <br> (A) injective (B) surjective <br> (C) bijective ( $D$ ) only injective | (C) |
| (26) | A cycle of length two is called .... <br> (A) identity permutation (B) transposition <br> (C) orbit (D) odd permutation | (B) |
| (27) | In the following permutation on 4-symbols, what is the value of $\sigma(3)$ ? $\sigma=\left(\begin{array}{llll} 1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3 \end{array}\right)$ <br> (A) 4 (B) 1 <br> (C) 2 (D) 3 | (A) |
| (28) | Statement: $\sigma=\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 1 & 3 & 4 & 1\end{array}\right)$ is a permutation. <br> This statement is.... <br> (A) True (B) False <br> (C) Can't say (D) None of these | (B) |
| (29) | The elements of a symmetric group $S_{3}$ can be interpreted as symmetries of a .... <br> (A) square (B) tetrahedron <br> (C) Triangle (equilateral) (D) None of these | (C) |
| (30) | The elements of a symmetric group $S_{4}$ can be interpreted as symmetries of a .... <br> (A) square (B) tetrahedron <br> (C) triangle (D) None of these | (B) |
| (31) | The elements of a symmetric group $D_{4}$ can be interpreted as symmetries of a .... | (A) |


|  | (A) square (B) tetrahedron <br> (C) triangle (D) None of these |  |
| :---: | :---: | :---: |
| (32) | $O\left(S_{n}\right)=\cdots$, where $S_{n}$ symmetric group of degree $n$. <br> (A) $(n-1)$ ! (B) $n$ ! <br> (C) $(n+1)!(D) \frac{n!}{2}$ | (B) |
| (33) | Cycle representation of $\sigma=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 5 & 3 & 1 & 4\end{array}\right) \in S_{n}$ is... <br> (A) (1254) <br> (B) $\left(\begin{array}{ll}2 & 5 \\ 1\end{array}\right)$ <br> (C) $(4125)$ (D) All of these | (D) |
| (34) | Two-line notation for a cycle (1354) in $S_{5}$ is..... <br> (A) $\sigma=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 5 & 3 & 1 & 4\end{array}\right)$ <br> (B) $\sigma=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 3 & 2 & 5 & 1 & 4\end{array}\right)$ <br> (C) $) \sigma=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 5 & 2 & 3 & 1 & 4\end{array}\right)$ <br> (D) $) \sigma=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 3 & 5 & 1 & 4\end{array}\right)$ | (B) |
| (35) | $O\left(S_{3}\right) \ldots$, where $S_{3}$ symmetric group of degree 3 . <br> (A) 2 (B) 4 <br> (C) 6 (D) 3 | (C) |
| (36) | Order of the permutation $\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 1 & 3 & 4 & 2\end{array}\right)$ is.... <br> (A) 3 (B) 4 <br> (C) 5 (D) 6 | (A) |
| (37) | Let $\sigma=\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3\end{array}\right)$ and $\tau=\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 3 & 2 & 1 & 4\end{array}\right)$ be two permutations on 4 symbols, then $\sigma \tau=\ldots$ <br> (A) $\left(\begin{array}{lll}1 & 2 & 3 \\ 2 & 1 & 4\end{array}\right.$ <br> (B) $\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 3 & 2 & 1 & 4\end{array}\right)$ <br> (C) $\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 1\end{array}\right)$ (D) $\left(\begin{array}{llll}1 & 2 & 3 & 4 \\ 4 & 1 & 2 & 3\end{array}\right)$ | (D) |
| (38) | Express the permutation $\sigma=\left(\begin{array}{lllllllll}1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 3 & 4 & 2 & 1 & 6 & 5 & 8 & 9 & 7\end{array}\right)$ as a product of disjoint cycles. <br> (A) (1324)(56) (B) (1324)(789) <br> (C) $(1324)(5)(6)(789)(D)(1324)(56)(789)$ | (D) |
| (39) | The single row representation of the permutation $\left(\begin{array}{llllll}1 & 2 & 3 & 4 & 5 & 6 \\ 2 & 3 & 5 & 6 & 1 & 4\end{array}\right)$ is... <br> (A) (1235)(46) (B) (123456) <br> (C) $(123651)(\mathrm{D})(125)(46)$ | (B) |
| (40) | The group $S_{n}$ is a finite group and is non-abelian if <br> (A) $n \geq 2$ <br> (B) $n>2$ <br> (C) $n \leq 2$ <br> (D) $n<2$ | (B) |


| 41) | The permutation $\sigma=\left(\begin{array}{ll}1 & 23 \\ 3 & 4\end{array} 456672\right)$ is .... <br> (A) an even permutation <br> (B) an odd permutation <br> (C) neither even nor odd permutation <br> (D) None of these | (B) |
| :---: | :---: | :---: |
| 42) | A permutation is called .......permutation if it can be expressed as a product of $\qquad$ number of transpositions. <br> (A) even, odd <br> (B) odd, even <br> (C) odd, odd <br> (D) none of these | (C) |
| 43) | The group $S_{n}$ of all permutations defined on $n$-symbols is called <br> (A) the symmetric group <br> (B) the non-symmetric group <br> (C) transposition <br> (D) abelian group | (A) |
| 44) | A permutation is called .......permutation if it can be expressed as a product of $\qquad$ number of transpositions. <br> (A) even, even <br> (B) even, odd <br> (C) odd, even <br> (D) none of these | (A) |
| 45) | If $S=\{1,2,3,4\}$ then, in $A_{4}$ how many permutations are there? <br> (A) 12 <br> (B) 21 <br> (C) 24 <br> (D) 4 | (A) |
| 46) | The alternating group is the group of all $\qquad$ .permutations. <br> (A) even <br> (B) odd <br> (C) both (A) and (B) <br> (D) none of these | (A) |
| 47) | $O\left(A_{4}\right)=\ldots$, where $A_{4}$ is the subgroup of $S_{4}$. <br> (A) 21 <br> (B) 12 <br> (C) 24 <br> (D) 6 | (B) |
| 49) | Identity permutation is always. $\qquad$ permutation. <br> (A) even <br> (B) odd <br> (C) neither even nor odd permutation <br> (D) none of these | (A) |
| 50) | The inverse of an odd permutation is $\qquad$ permutation. <br> (A) even <br> (B) neither even nor odd permutation <br> (C) odd <br> (D) none of these | (C) |
| 51) | The value of $\sigma(4)$ if $\sigma=\left(\begin{array}{ll}1 & 4\end{array} 2\right)$ (A) 1 <br> (B) 2 <br> (C) 4 <br> (D) 3 | (D) |
| 52) | The inverse of (1234) is <br> (A) (4321) <br> (B) $(2341)$ <br> (C) (1234) <br> (D) $(1432)$ | (A) |
| 53) | If $R$ is a ring then trivial subrings of $R$ are $\ldots$ <br> (A) $\{0\}$ <br> (B) $R$ <br> (C) $\{0\}$ and $R$ <br> (D) none of these | (C) |
| 54) | Let $I_{1}$ and $I_{2}$ are any two ideal of a ring $R$, then which of the following is incorrect? <br> (A) $I 1 \cup I 2$ is an ideal of $R$ | (A) |


|  | (B) $I_{I} \cap I_{2}$ is an ideal of $R$ <br> (C) $I_{1}+I_{2}$ is an ideal of $R$ <br> (D) $I_{1} I_{2}$ is an ideal of $R$ |  |
| :---: | :---: | :---: |
| 55) | If $I$ is an ideal in a ring $R$, then.... <br> (A) $\frac{I}{R}$ is a ring <br> (B) $\frac{R}{I}$ is a ring <br> (C) $R I$ is a ring <br> (D) None of these | (B) |
| 56) | If $R$ is a commutative ring with unit element, $M$ is an ideal of $R$ and $\frac{R}{M}$ is a field, then <br> (A) $M$ is minimal ideal of $R$ <br> (B) $M$ is maximal ideal of $R$ <br> (C) $M$ is not a maximal ideal of $R$ <br> (D) None of these | (B) |
| 57) | If $R$ is a commutative ring with unit element, then <br> (A) every maximal ideal is prime ideal <br> (B) every prime ideal is maximal ideal <br> (C) every ideal is prime ideal <br> (D) every ideal is maximal ideal | (A) |
| 58) | If $R$ is a finite commutative ring, then <br> (A) every maximal ideal is prime ideal <br> (B) every prime ideal is maximal ideal <br> (C) every ideal is prime ideal <br> (D) every ideal is maximal ideal | (B) |
| 59) | Let $H_{4}=\{4 n / n \in \mathbb{Z}\}$ is a $\qquad$ .ideal in the ring of even integers. <br> (A) maximal <br> (B) prime <br> (C) neither prime nor maximal <br> (D) none of these | (A) |
| 60) | Let $H_{4}=\{4 n / n \in \mathbb{Z}\}$ is a $\qquad$ ideal in the ring of integers. <br> (A) maximal <br> (B) prime <br> (C) neither prime nor maximal <br> (D) none of these | (C) |
| 61) | If $R=\mathbb{Z}_{6}$ then $I=\{\overline{0}, \overline{3}\}$ is a... <br> (A) ideal in $R=\mathbb{Z}_{6}$ <br> (B) not ideal in $R=\mathbb{Z}_{6}$ <br> (C) ideal in $R=\mathbb{Z}$ <br> (D) None of these | (A) |
| 62) | Choose the ideals in a ring $R=\mathrm{Z}$. <br> (A) $I=2 \mathbb{Z}$ <br> (B) $I=3 \mathbb{Z}$ <br> (C) $I=5 \mathbb{Z}$ <br> (D) All of these | (D) |
| 63) | Which of the following is prime ideal of a ring $R=\mathbb{Z}$. <br> (A) $I=4 \mathbb{Z}$ <br> (B) $I=6 \mathbb{Z}$ <br> (C) $I=5 \mathbb{Z}$ <br> (D) All of these | (C) |
| 64) | A non-empty subset $S$ of a ring $R$ is a subring of $R$ if and only if | (C) |


|  | $a, b \in S$, then <br> (A) only $a b \in S$ <br> (B) only $a-b \in S$ <br> (C) $a b \in S$ and $a-b \in S$ <br> (D) none of these |  |
| :---: | :---: | :---: |
| 65) | Consider a quotient ring $\frac{\mathbb{Z}}{H_{4}}=\left\{H_{4}, H_{4}+1, H_{4}+2, H_{4}+3\right\},$ <br> Where, $\left\{H_{4}=4 n / n \in \mathbb{Z}\right\}$ and $(\mathbb{Z},+, *)$ is the ring of integers. The additive identity in the quotient ring $\frac{\mathbb{Z}}{H_{4}}$ is.... <br> (A) $\mathrm{H}_{4}+1$ <br> (B) $\mathrm{H}_{4}$ <br> (C) $H_{4}+2$ <br> (D) $H_{4}+3$ | (B) |
| 66) | The ring $(\mathbb{Z},+, *)$ has unity1, but its subring ( $\mathrm{E},+, *$ ) of even integers has..... <br> (A) unity 1 <br> (B) unity 2 <br> (C) unity 0 <br> (D) no unity | (D) |
| 67) | If $R=$ Ring of integers, then characteristic of $R$ is... <br> (A) 0 <br> (B) 1 <br> (C) 2 <br> (D) 3 | (A) |
| 68) | The characteristic of the ring of integers $(R)$ and ring of even integers $(E)$ is such that <br> (A) $\operatorname{ch} R<c h E$ <br> (B) $\operatorname{ch} R \neq c h E$ <br> (C) $\operatorname{ch} R>c h E$ <br> (D) $c h R=c h E$ | (D) |
| 69) | What is the characteristic of the ring of even integers? <br> (A) 6 <br> (B) 4 <br> (C) 2 <br> (D) 0 | (D) |
| 70) | The characteristic of the ring $\mathbb{Z}_{6}$ is $\ldots$ <br> (A) 6 <br> (B) 5 <br> (C) 2 <br> (D) 3 | (A) |
| 71) | If integral domain $D$ is of finite characteristic, then its characteristic is..... <br> (A) odd number <br> (B) even number <br> (C) prime number <br> (D) natural number | (C) |
| 72) | A non-empty subset $I$ of a ring $R$ is called a right ideal of $R$ if <br> (A) $a, b \in I \Rightarrow a-b \in I$ <br> (B) $a \in I, r \in R \Rightarrow a r \in I$ <br> (C) $a \in I, r \in R \Rightarrow r a \in I$ <br> (D) both (A) and (B) | (B) |
| 73) | Read the following statements and choose the correct option. <br> Statement I: An ideal is always a subring. <br> Statement II: A subring may not be an ideal. <br> (A) Only statement I is true <br> (B) Only statement II is true <br> (C) Both (A) and (B) are true <br> (D) None of these | (C) |
| 74) | If $\theta: R \rightarrow R^{\prime}$ be a homomorphism (where $R$ and $R^{\prime}$ be the two rings with 0,0 as zeros respectively) then <br> (A) $\theta(0)=0^{\prime}, \theta(-a)=-a$ <br> (B) $\theta(0)=0, \theta(-a)=-a$ <br> (C) $\theta(0)=0^{\prime}, \theta(-a)=a$ <br> (D) $\theta\left(0^{\prime}\right)=0, \theta(-a)=-a$ | (A) |


| 75) | Let $(R,+, *),\left(R^{\prime}, *, o\right)$ be two rings. A mapping $\theta: R \rightarrow R^{\prime}$ is called a homomorphism if for any $a, b \in R$. <br> (A) $\begin{gathered} \theta(a+b)=\theta(\mathrm{a})+\theta(\mathrm{b}) \\ \theta(a * b)=\theta(\mathrm{a}) * \theta(\mathrm{~b}) \end{gathered}$ <br> (B) $\theta(a+b)=\theta(\mathrm{a}) * \theta(\mathrm{~b})$ <br> $\theta(a * b)=\theta(\mathrm{a}) o \theta(\mathrm{~b})$ <br> (C) $\theta(a+b)=\theta(\mathrm{a})+\theta(\mathrm{b})$ <br> (D) $\theta(a * b)=\theta(\mathrm{a}) o \theta(\mathrm{~b})$ | (B) |
| :---: | :---: | :---: |
| 76) | Let $f: R \rightarrow R^{\prime}$ be a homomorphism of $R$ onto $R^{\prime}$ with $\operatorname{ker} f=0$. Then $f$ is.... <br> (A) an endomorphism <br> (B) an isomorphism <br> (C) an automorphism <br> (D) none of these | (B) |
| 77) | Let $f: R \rightarrow R^{\prime}$ be a homomorphism of $R$ in $R^{\prime}$. Then $f$ is a one-one map if and only if <br> (A) $\operatorname{ker} f>0$ <br> (B) $\operatorname{ker} f<0$ <br> (C) $\operatorname{ker} f=0$ <br> (D) none of these | (C) |
| 78) | Read the following statement and choose the correct option. Statement: Let $R=Z$ (ring) and $P=p Z$ (ideal), where, $p$ is a prime. Then $P$ is a prime ideal in the ring $R$. <br> (A) False <br> (B) True <br> (C) Can't say <br> (D) None of these | (B) |
| 79) | Read the following statement and choose the correct option. <br> Statement: For any ideals $I$ and $J$ of a ring $R$, the sum $I+J$ and the product $I J$ are ideals in a ring $R$. <br> (A) True <br> (B) False <br> (C) Can't say <br> (D) None of these | (A) |
| 80) | Two polynomials $f(x)=a_{0}+a_{1} x+a_{2} x^{2}+\cdots+a_{n} x^{n}, a_{n} \neq 0 \text { and } g(x)=b_{0}+$ $b_{1} x+b_{2} x^{2}+\cdots+b_{n} x^{n}, b_{n} \neq 0$ will be equal if and only if <br> (A) $m=n$ <br> (B) $a_{i}=b_{i} \forall i$ <br> (C) both (A) and (B) <br> (D) none of these | (C) |
| 81) | If the ring $R$ is an integral domain, then <br> (A) $R[x]$ is an integral domain <br> (B) $R[x]$ is not an integral domain <br> (C) $R[x]$ is a field <br> (D) $R[x]$ is a commutative division ring | (A) |
| 82) | Read the following statements and choose the correct option. Let $R[x]$ be the ring of polynomials over a ring $R$ then <br> Statement $I: R$ is commutative if and only if $R[x]$ is commutative. <br> Statement II: $R$ has unity if and if $R[x]$ has unity. <br> (A) Only statement I is true <br> (B) Only statement II is true <br> (C) Both (A) and (B) are true <br> (D) None of these | (C) |
| 83) | Over the field of real numbers the polynomial $x^{2}+25$ is <br> (A) irreducible <br> (B) reducible | (A) |


|  | (C) neither reducible nor reducible <br> (D) none of these |  |
| :---: | :---: | :---: |
| 84) | Let $f(x)=1+2 x-2 x^{2}$ and $g(x)=2+3 x+2 x^{2}$ be two members of $Z[x]$, then degree of $f(x)+g(x)=\ldots$ <br> (A) 0 <br> (B) 1 <br> (C) 4 <br> (D) 5 | (B) |
| 85) | Consider the ring $R=\{0,1,2,3,4,5\}$ modulo6 and $f(x)=1+2 x^{3}, g(x)=2+x-3 x^{2}$ be two polynomials in $R[x]$ of degree 3 and 2 respectively. Then degree of $f(x)+g(x)=\ldots$ <br> (A) 0 <br> (B) 1 <br> (C) 5 <br> (D) 4 | (D) |
| 86) | Which of the following polynomials of $Z[x]$ are irreducible over $Z$. <br> (A) $x^{2}+1$ <br> (B) $x^{2}+4$ <br> (C) $x^{2}+25$ <br> (D) All of these | (D) |
| 87) | $f(x) \in F[x]$ a polynomial of degree 2 or 3 is reducible if and only if $a \in F$ such that <br> (A) $f(a)=0$ <br> (B) $f(a) \neq 0$ <br> (C) $f(a)>0$ <br> (D) $f(a)<0$ | (A) |
| 88) | The fact that $f(a)=0$ is also expressed by saying that $a$ is $\qquad$ <br> $(\mathrm{A})$ a root of the polynomial $f(x)$. <br> (B) a factor of the polynomial $f(x)$. <br> (C) both (A) and (B) <br> (D) None of these | (A) |
| 89) | The polynomial $1+x+2 x^{2}$ in $Z_{3}[x]$ <br> (A) is irreducible <br> (B) is reducible <br> (C) is neither reducible nor reducible <br> (D) none of these | (A) |
| 90) | Over the field of complex numbers the polynomial $x^{2}+16$ is <br> (A) irreducible <br> (B) reducible <br> (C) neither reducible nor reducible <br> (D) none of these | (B) |
| 91) | Over the field of rational numbers the polynomial $x^{2}+2$ is <br> (A) irreducible <br> (B) reducible <br> (C) neither reducible nor reducible <br> (D) none of these | (A) |
| 92) | Which of the following(s) is/are reducible over. <br> (A) $x^{2}+16$ <br> (B) $x^{2}+25$ <br> (C) $x^{2}+1$ <br> (D) All of these | (D) |
| 93) | Which of the following is irreducible over $\mathbb{Z}$. <br> (A) $x^{2}-5 x+6$ <br> (B) $x^{2}-7 x+12$ <br> (C) $x^{2}-9 x+20$ <br> (D) None of these | (D) |


| 94) | Read the following statement and choose the correct option. Any polynomial of degree 1 is irreducible over a field $F$. <br> (A) False <br> (B) True <br> (C) Can't say <br> (D) None of these | (B) |
| :---: | :---: | :---: |
| 95) | Which of the following(s) is/are reducible over $\mathbb{Z}$. <br> (A) $x^{2}-5 x+6$ <br> (B) $x^{2}-7 x+12$ <br> (C) $x^{2}-9 x+20$ <br> (D) None of these. | (D) |
| 96) | The polynomial $x^{4}+x+1$ in $Z_{2}[x]$ <br> (A) is irreducible <br> (B) is reducible <br> (C) is neither reducible nor reducible <br> (D) none of these | (B) |
| 97) | Let $f(x)=a_{0}+a_{1} x+a_{2} x^{2}+\cdots+a_{n} x^{n}$ be a polynomial with integer's coefficients (i.e. $f(x) \in R[x]$ ). Suppose that for some prime number $p$, $p\left\|a_{0}, p\right\| a_{1}, \ldots, p\left\|a_{n-1}, p\right\| a_{n}, p^{2} \mid$ then $f(x)$ is $\ldots \ldots .$. polynomial over the ring of rationals. <br> (A) neither reducible nor reducible <br> (B) reducible <br> (C) irreducible <br> (D) none of these | (C) |
| 98) | Let $f(x)=a_{0}+a_{1} x+a_{2} x^{2}+\cdots+a_{m} x^{m}$ be any non-zero polynomial in $R[x]$. Then $f(x)$ has degree $m$ if <br> (A) $a_{m} \neq 0, a_{i}=0 \forall i>m$ <br> (B) $a_{m}=0, a_{i} \neq 0 \forall i>m$ <br> (C) $a_{m}=0, a_{i}=0 \forall i>m$ <br> (D) $a_{m} \neq 0, a_{i} \neq 0 \forall i>m$ | (A) |
| 99) | The polynomial $a_{0}+a_{1} x+a_{2} x^{2}=2+4 x+x^{2}$ is irreducible over $Q$, if we take <br> (A) $p=2$ <br> (B) $p=3$ <br> (C) $p=7$ <br> (D) $p=4$ | (A) |
| 100) | The polynomial $f(x)$ is divisible by $x-a$ then $\mathrm{f}(\mathrm{a})=\ldots$ <br> (A) 2 <br> (B) 5 <br> (C) 0 <br> (D) a | (C) |
| 101) | If $f(x)=1+2 x+3 x^{2}$ and $g(x)=7 x+2 x^{2}+3 x^{3}$ are two polynomials over $\left(\mathbb{Z}_{6},+_{6}, *_{6}\right)$ then $\operatorname{deg}(f(x)+g(x))=\ldots$. <br> (A) 2 <br> (B) 3 <br> (C) 5 <br> (D) 4 | (B) |
| 102) | The zeros of the polynomial $x^{2}-4 x-12$ over field of real numbers are <br> (A) $3,-4$ <br> (B) $6,-2$ <br> (C) $-6,2$ <br> (D) $-3,4$ | (B) |
| 103) | The characteristic of the ring ( $3 \mathbb{Z},+, \times$ ) is.... <br> (A) 3 <br> (B) $n$ | (C) |


|  | (C) 0 (D) none of these |  |
| :---: | :---: | :---: |
| 104) | If $F$ is a field then $F[x]$ is... <br> (A) an integral domain <br> (B) a field <br> (C) may not be field <br> (D) none of these | (A) |
| 105) | The zeros of the polynomial $x^{2}-4 x-12$ over the field of real numbers are.... <br> (A) 1,2 <br> (B) 2, 3 <br> (C) 4,3 <br> (D) $-4,-3$ | (C) |
| 106) | The characteristic of ring integers $\left(\mathbb{Z},+,{ }^{*}\right)$ is.... <br> (A) 2 <br> (B) a prime number <br> (C) zero <br> (D) none of these | (C) |
| 107) | If $f(x)=2 x^{3}+x^{2}+3 x-2$ and $g(x)=3 x^{4}+2 x+4$ be two polynomials over $\mathbb{Z}_{6}$, then $\operatorname{deg}(f(x) * g(x))=\ldots$. <br> (A) 5 <br> (B) 6 <br> (C) 7 <br> (D) none of these | (A) |
| 108) | Let $f(x)=2 x^{3}+4 x^{2}+3 x+3$ be a polynomial over $\mathbb{Z}_{5}$ then $f$ <br> (4) $=$... <br> (A) 0 <br> (B) 2 <br> (C) 4 <br> (D) 1 | (B) |
| 109) | The characteristic of Boolean ring is... <br> (A) 0 <br> (B) 2 <br> (C) 4 <br> (D) 1 | (B) |
| 110) | If $f(x) \in F[x]$ and $a \in F$, for a field $F$, then $x-a$ divides $f(x)$ if and only if <br> (A) $f(a)=0$ <br> (B) $f(a) \neq 0$ <br> (C) $f(a)=1$ <br> (D) $f(a)=\infty$ | (A) |

